








MARVEL analysis of high-resolution rovibrational spectra of $^{16}\text{O}^{12}\text{C}^{18}\text{O}$

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Abstract

Empirical rovibrational energy levels are presented for the third most abundant, asymmetric carbon dioxide isotopologue, $^{16}\text{O}^{12}\text{C}^{18}\text{O}$, based on a compiled dataset of experimental rovibrational transitions collected from the literature. The 52 literature sources utilized provide 19,438 measured lines with unique assignments in the wavenumber range of 2–12,676 cm^{-1} . The MARVEL (Measured Active Rotational-Vibrational Energy Levels) protocol, which is built upon the theory of spectroscopic networks, validates the great majority of these transitions and outputs 8786 empirical rovibrational energy levels with an uncertainty estimation based on the experimental uncertainties of the transitions. Issues found in the literature data, such as misassignment of quantum numbers, typographical errors, and misidentifications, are fixed before including them in the final MARVEL dataset and analysis. Comparison of the empirical energy-level data of this study with those in the line lists CDSD-2019 and Ames-2021 shows good overall agreement, significantly better for CDSD-2019; some issues raised by these comparisons are discussed.

KEYWORDS

CO_2 , line positions, MARVEL, rovibrational energy levels

1 | INTRODUCTION

Numerous scientific and engineering domains, including atmospheric science,¹ climate modeling,² astrophysics,³ and gas laser technology,^{4,5} benefit from knowledge about the high-resolution rovibrational spectroscopy of isotopologues of carbon dioxide, CO_2 . Studying CO_2 in planetary atmospheres, including those of our neighboring terrestrial planets, Venus⁶ and Mars,⁷ provides insight into the time evolution of atmospheres⁸: a detailed understanding of how CO_2 abundance has changed over time on various planets sheds light on factors that influence the stability and composition of atmospheres.

Although CO_2 spectra are often dominated by the parent isotopologue (hereafter the original HITRAN isotopologue [AFGL, Air Force Geophysics Laboratory] shorthand codes, like 626 for $^{12}\text{C}^{16}\text{O}_2$, will be used), understanding fine details about the spectra of isotopologues of CO_2 is also highly relevant. To underline this statement, note that (a) isotopic abundances vary around the Universe and the isotopic composition of CO_2 is known to vary significantly in different regions of space, and (b) it is well established that the atmospheric absorptions on Earth associated with 626 are saturated (in other words, these lines are optically thick⁹), but this is not true in general for the other CO_2 isotopologues. Asymmetric CO_2 isotopologues, such as $^{16}\text{O}^{12}\text{C}^{18}\text{O}$ (628), are particularly important in this regard,

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since one of the effects of isotopic substitution is that it breaks the symmetry dictated by the two equivalent ^{16}O atoms in 626. This has significant consequences for the (ro)vibrational selection rules and, as a result, leads to new lines and shifts in the rovibrational spectra. Probably the most important effect of the isotopic substitution of one of the O atoms of carbon dioxide is that for 628 all rotational states are allowed, in contrast to 626 (or 636, which we have studied recently¹⁰), for which half of the states are forbidden by the Pauli principle. Thus, asymmetric isotopologues of CO_2 have significantly more spectral lines and, importantly, lines in ranges where 626 does not absorb.

The importance of the spectra of asymmetric CO_2 isotopologues has led to the development of theories to treat their vibrational motion¹¹ and the construction of rovibrational line lists of varying accuracy and size.^{12–15} The rovibrational spectra of 628 have been studied using high-resolution and precision spectroscopic techniques.^{16–72} These are the experimental studies considered in detail during this investigation.

The principal aim of the present computational study is the provision of large sets of validated measured line positions and accurate empirical rovibrational energies for 628. This is achieved through the use of the MARVEL (measured active rotational-vibrational energy levels) procedure,^{73–75} built upon the theory of spectroscopic networks.^{76,77} The datasets created during this study may also be used to improve theoretical models, can supplement variational nuclear-motion calculations, and improve line lists, like HITRAN⁷⁸ and ExoMol.⁷⁹

2 | THEORETICAL BACKGROUND

2.1 | MARVEL

The MARVEL procedure^{73–75} involves the careful identification and collection, the critical examination, and the thorough validation of high-resolution laboratory spectral data, with emphasis on the position of the lines. To be included in the MARVEL input file, a spectral line has to have not only an accurate position, but also unique labels for the upper and the lower energy levels and an associated uncertainty value. These spectral lines are then used to construct a spectroscopic network (SN), wherein each energy level serves as a vertex of the SN, and the vertices are interconnected with observed transitions (thus, they are the edges of the SN). This SN allows, via an inversion of the information contained in the measured lines, the determination of empirical energy-level values along with educated estimates for their uncertainties.⁸⁰

Ideally, one would create a well-connected SN linking all transitions to the ground state (the state with no rovibrational excitation, the root of the SN). However, due to the availability of incomplete experimental data, this is not usually feasible. In practice, the SN becomes fragmented, resulting in a principal component, where all the vertices are linked to the ground state, and a number of isolated, so-called floating components.^{81,82} The very nature of these floating components makes it uncertain whether their constituent lines align

with all the other spectroscopic data, meaning that these lines remain “unvalidated” at the end of a MARVEL analysis. When floating components contain a substantial number of transitions, it may be desirable to connect them to the principal component(s) using accurate (semi-)empirical lines.

Since MARVEL is not constrained by detailed theoretical model assumptions, it is not affected by perturbations of energy levels caused by so-called accidental resonances. However, it can accept transitions that may be considered “illegal” (e.g., not complying with well-established selection rules), as long as they are not in conflict with the rest of the data entering the analysis. Hence, it is crucial to continuously screen the experimental dataset for incorrect transitions during the construction of the MARVEL input. MARVEL can detect inconsistencies,^{82–84} that is lines which significantly deviate from the majority of the data provided. This feature proves invaluable for identifying issues with the experimental data, whether stemming from user mistakes during data collection and analysis or from misassignments.

2.2 | Rovibrational quantum numbers

To ensure that MARVEL can successfully validate the measured transitions, labeling of the energy levels involved must be consistent across the entire dataset. In this work, as in our 636 study,¹⁰ we adopt the AFGL notation^{47,85,86} for the description of the vibrational quantum states of CO_2 . This notation uses five descriptors, ν_1 , ν_2 , l_2 , ν_3 , and r , and avoids the use of super- and sub-scripts, and thus makes the notation well suited to electronic databases. In this notation the vibrational states are described by four quantum numbers and a counting number: ν_1 and ν_3 correspond to the “symmetric” and “antisymmetric” stretches, ν_2 to the linear bend, l_2 is the angular momentum associated with the linear bending, and r is the so-called Fermi-resonance ranking index, which can range from 1 to $\nu_1 + 1$.^{47,87,88} In the “standard” harmonic oscillator (HO) notation, $\nu_1\nu_2^2\nu_3$, l_2 and ν_3 are the same as in the AFGL notation. The AFGL notation can be related straightforwardly to the HO notation: for states mixed by the effects of Fermi-resonance, $\nu^{\text{AFGL}} = \nu^{\text{HO}} + (r - 1)$ and $\nu^{\text{AFGL}} = \nu^{\text{HO}} - 2(r - 1)$.⁸⁷ Thus, for example, the state $2\ 0^0\ 0$ in HO notation corresponds to $2\ 0\ 0\ 0\ 1$ in AFGL, while $1\ 2^0\ 0 \equiv 2\ 0\ 0\ 0\ 2$ and $0\ 4^0\ 0 \equiv 2\ 0\ 0\ 0\ 3$.⁸⁶

Besides the five vibrational descriptors utilized in the AFGL notation, there are two more descriptors characterizing a rovibrational quantum state of carbon dioxide, namely the rotational quantum number J and the rotationless parity p , the latter denoted here as either “e” or “f”.⁸⁹ Thus, the complete label of a rovibrational energy level adopted in this study is $(J\ \nu_1\ \nu_2\ l_2\ \nu_3\ r\ p)$. It is worth noting that in the AFGL notation the quantum numbers ν_2 and l_2 are always equal.⁹⁰ The AFGL notation has the advantage, as shown by Amat and Pimbert,⁸⁵ that while with the use of the standard notation the order of the rovibrational energy levels can change between isotopologues, in the AFGL notation this is not the case, though at the expense of the introduction of a redundant quantum number.

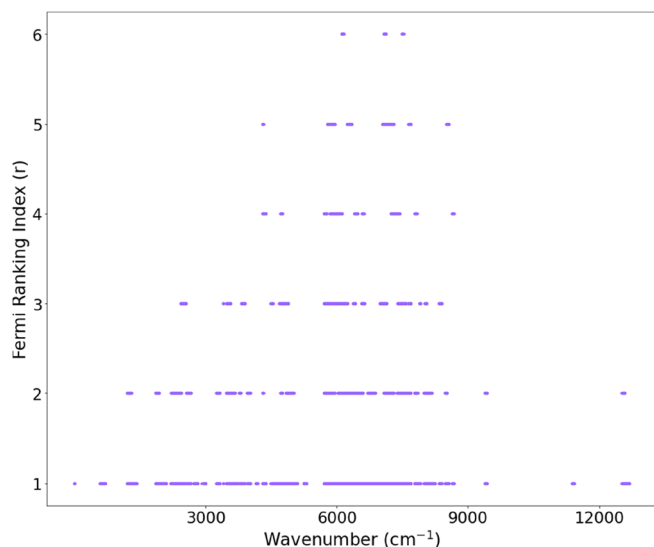


FIGURE 1 Distribution of the Fermi ranking index, r , of our final energy levels across the experimental spectral region covered.

It must also be mentioned that besides Fermi resonances there are various other types of resonances affecting the infrared spectra of CO_2 , such as Coriolis and ℓ -type resonances.^{91,92} These resonance effects contribute to the complexity of the spectral patterns and complicate the labeling of the energy levels. Nevertheless, Fermi resonances including overtones and combinations of the ν_1 and $2\nu_2$ states remain the most important interactions. Figure 1 illustrates the spectral ranges affected by Fermi resonances in the experimental spectrum. The effect is considerable across the entire spectrum, with some regions above 6000 cm^{-1} having up to six resonating bands.

2.3 | Selection rules

For all asymmetric CO_2 isotopologues the equilibrium geometry belongs to the $C_{\infty v}$ point group. The selection rules for one-photon dipole-allowed rovibrational transitions among the quantum states of 628 can be summarized as follows. For rotational transitions, $\Delta J = 0, \pm 1$, and when

$$\Delta J = 0; e \leftrightarrow f, \quad (1)$$

that is the rotationless parity changes between the initial and the final states in the Q branch, while if

$$\Delta J = \pm 1; e \leftrightarrow e, f \leftrightarrow f, \quad (2)$$

that is in the P and R branches there is no parity change. Furthermore, non-degenerate vibrational states with $l_2 = 0$ all have e parity (thus, in some sources the parity information is not given explicitly), while vibrational states with $l_2 > 0$ support both an e- and an f-parity state for each J .

2.4 | Dataset construction

We closely follow the methodology described in our earlier study of the high-resolution spectroscopy of the 636 isotopologue of CO_2 .¹⁰ Briefly, the method begins with a primary classification of the sources gathered, based on their experimental uncertainty, as well as the accuracy, self-consistency, and overall quality of the transitions reported. After a master dataset is built using data taken from the best sources, the rest of the sources are added carefully, while actively quarantining lines whose addition results in data conflicts. After this step, the quarantined lines are carefully inspected for possible errors, such as typos and misassignments. The errors detected are fixed and then the transition is added to the input dataset. The lines remaining under quarantine are removed from the final MARVEL analysis. These lines are marked with a minus sign in front of the wavenumber entry, as can be seen in the [Supplementary Material](#).

After all the experimental data available are successfully included, or perhaps refuted, in the input dataset, a spectroscopic network is created from them. This SN, as usual, is fragmented, that is, it includes many floating components. In the case of carbon dioxide, including 628, the CDS-2019¹⁴ line list contains results from accurate semi-empirical calculations; hence, we used transitions from this dataset to connect floating components to the principal one.

Following the inclusion of the majority of the observed transitions in the principal component, analysis of the uncertainties of the lines and then the energy levels was undertaken. Uncertainties of some of the lines have been increased based on recommendations of the MARVEL procedure, until self-consistency is achieved for the input dataset. This is followed by the generation of the empirical rovibrational energy levels. Finally, the empirical energy levels are compared to their counterparts in existing datasets,^{14,15,78} further searching for outliers. This last step also ensures the consistency of the energy-level labels across all datasets and identifies potential conflicts not detected by MARVEL.

3 | EXPERIMENTAL STUDIES OF $^{16}\text{O}^{12}\text{C}^{18}\text{O}$ LINE POSITIONS

After a thorough search of the literature, we found 59 sources containing assigned experimental line positions for 628. Seven of these sources were assessed to be unusable and eventually were excluded from the MARVEL analysis. The specifics why these data are not used are discussed in Section 3.2. Characteristics of the 52 literature sources utilized, containing altogether 33,755 rovibrational transitions (19,438 unique ones), are summarized in Table 1. As detailed in Section 2.4, all the lines in the database underwent comprehensive processing and analysis, utilizing the fourth generation of the MARVEL code, which uses a bootstrap method to determine the uncertainty in the final energy levels.⁸⁰ Section 3.3 provides specific comments on some of the entries of Table 1.

TABLE 1 Experimental sources of rovibrational transitions of $^{16}\text{O}^{12}\text{C}^{18}\text{O}$ and some characteristics of the lines they contain.

Source	Range/cm ⁻¹	A/V/D ^a	CSU ^b	MSU ^c	Notation
80EnYoSaHo ²⁶	2.21–5.89	5/5/0	1.7×10^{-6}	1.7×10^{-6}	Other
80PaKaAn ²⁸	624.52–702.51	118/118/0	1.2×10^{-3}	2.6×10^{-3}	Other
85Jolma ³⁵	632.90–696.32	92/91/1	5.0×10^{-4}	5.1×10^{-4}	Other
86GuRa ⁴⁰	644.22–2355.26	87/87/0	5.0×10^{-4}	5.2×10^{-4}	Other
86BrSoFr ⁹⁴	933.72–1094.35	98/98/0	4.3×10^{-7}	4.3×10^{-7}	Other
85Toth ³⁷	1212.73–1416.49	371/371/0	5.0×10^{-4}	5.3×10^{-4}	AFGL
83BeRiRiSo ²⁹	1859.38–1868.55	3/3/0	1.0×10^{-4}	1.0×10^{-4}	AFGL
85RiBeDe ³⁶	1859.38–1931.68	36/34/2	1.0×10^{-3}	1.1×10^{-3}	AFGL
84RiBeDeFe ³⁴	1862.90–2659.60	851/849/2	1.0×10^{-3}	1.6×10^{-3}	AFGL
12LyKaJaLu ⁵⁴	1865.02–6937.38	3372/3372/0	1.0×10^{-3}	1.2×10^{-3}	AFGL
84RiBe ³³	2004.91–2096.71	92/92/0	1.0×10^{-3}	1.3×10^{-3}	AFGL
12JaGuLyKa ⁵³	2019.93–5066.98	436/436/0	1.0×10^{-4}	1.3×10^{-4}	AFGL
86RiBeDe ⁴¹	2068.89–2103.72	18/18/0	1.0×10^{-3}	1.8×10^{-3}	AFGL
83EsRo ³⁰	2200.87–2377.59	1042/1036/6	1.2×10^{-3}	1.5×10^{-3}	AFGL
86EsSaRoVa ³⁹	2213.38–3721.75	1347/1344/3	9.7×10^{-4}	1.8×10^{-3}	AFGL
84BaRo ³¹	2268.99–2369.42	214/207/7	1.0×10^{-4}	3.0×10^{-4}	AFGL
15EISuMi ⁶⁰	2270.11–2368.45	79/79/0	3.0×10^{-6}	3.2×10^{-6}	Other
78BaDeChRa ²⁴	2270.74–2367.06	219/219/0	3.0×10^{-3}	4.9×10^{-3}	Other
80Guelachv ²⁷	2288.26–2361.92	95/95/0	1.5×10^{-4}	4.9×10^{-4}	Other
68ObRaHaMc(P) ²¹	2298.17–2359.68	88/83/5	2.9×10^{-2}	3.1×10^{-2}	Other
68ObRaHaMc(O) ²¹	2298.19–2359.69	78/78/0	2.5×10^{-2}	3.0×10^{-2}	Other
84DeRiBe ³²	2398.34–2659.60	466/464/2	1.0×10^{-3}	1.5×10^{-3}	AFGL
07ToMiBrDe ⁴⁵	2458.74–6937.01	1548/1548/0	4.8×10^{-4}	5.0×10^{-4}	AFGL
78RoFiBuCa ²⁵	2485.42–2640.19	81/81/0	1.5×10^{-2}	1.7×10^{-2}	AFGL
08ViMuNoHe ⁶	2962.23–3000.13	47/47/0	1.0×10^{-2}	1.3×10^{-2}	AFGL
14BoJaLyTa ⁵⁷	3239.74–4662.39	1576/1572/4	1.7×10^{-4}	3.5×10^{-4}	AFGL
88BeDeRiFe ⁴²	3290.58–3314.03	21/21/0	1.0×10^{-3}	2.1×10^{-3}	AFGL
71ObRa ²²	3526.20–3705.35	173/173/0	3.0×10^{-3}	7.3×10^{-3}	AFGL
65GoRo ¹⁸	3549.25–3695.38	55/55/0	5.0×10^{-3}	6.8×10^{-3}	Other
08WaPeTaSo ⁴⁸	3816.94–8235.96	3434/3433/1	1.1×10^{-3}	1.5×10^{-3}	AFGL
16VaKoMoKa ⁶⁵	4298.32–4378.04	531/531/0	2.0×10^{-3}	2.3×10^{-3}	AFGL
22MaBoPeSo ⁷¹	4477.19–4540.00	22/22/0	3.0×10^{-3}	3.0×10^{-3}	AFGL
99KsGiChBr ⁴³	4593.69–4660.99	69/69/0	1.0×10^{-3}	1.0×10^{-3}	AFGL
15BoJaLyTa ⁵⁹	4696.28–5286.92	849/848/1	1.9×10^{-4}	4.5×10^{-4}	AFGL
16BeDeSuBr ⁶³	4704.18–4933.17	632/559/73	1.7×10^{-3}	4.5×10^{-3}	AFGL
23FICeCaKa ⁷²	4895.58–4913.17	2/2/0	1.2×10^{-7}	1.2×10^{-7}	AFGL
18KaCeMoKa ⁶⁹	5703.45–5878.71	1253/1253/0	1.1×10^{-3}	1.2×10^{-3}	AFGL
18CeKaMoKa ⁶⁸	5731.90–5878.59	540/540/0	1.0×10^{-3}	1.2×10^{-3}	AFGL
08PeKaPeTa ⁴⁶	5851.82–6937.40	852/852/0	2.1×10^{-3}	2.3×10^{-3}	AFGL
13KaCaMoBe ⁵⁵	5851.82–6937.40	6426/6425/1	1.0×10^{-3}	1.2×10^{-3}	AFGL
06PeKaRoPe ⁴⁴	5957.55–6832.25	443/443/0	1.5×10^{-3}	1.8×10^{-3}	AFGL
15JaBoLyTa ⁶¹	6090.52–6283.26	150/150/0	3.0×10^{-4}	4.2×10^{-4}	AFGL
16DeBeSuBr ⁶⁴	6120.09–6151.99	45/45/0	6.7×10^{-4}	1.4×10^{-3}	AFGL
05MaMaRoPe ⁹⁵	6132.73–6496.25	593/589/4	3.0×10^{-3}	3.3×10^{-3}	AFGL
17KaKaTaPe ⁶⁷	6977.92–7913.89	3429/3429/0	1.0×10^{-3}	1.2×10^{-3}	AFGL
09KaSoCa ⁵⁰	7123.01–7650.24	375/375/0	5.0×10^{-4}	9.0×10^{-4}	AFGL

TABLE 1 (Continued)

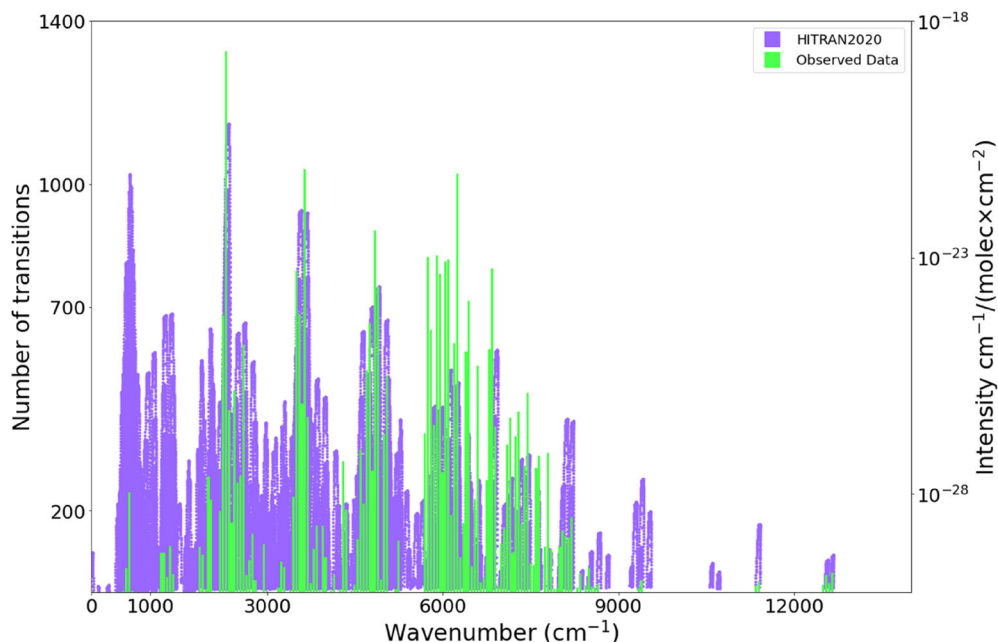
Source	Range/cm ⁻¹	A/V/D ^a	CSU ^b	MSU ^c	Notation
10SoKaTaPe ⁵²	7128.15–7650.24	369/369/0	1.1×10^{-3}	1.3×10^{-3}	AFGL
10CaSoMoPe ⁵¹	7316.45–7478.78	17/17/0	8.0×10^{-4}	8.7×10^{-4}	AFGL
14KaKaTaPe ⁵⁸	7985.91–8235.93	548/548/0	1.0×10^{-3}	1.2×10^{-3}	AFGL
20KaKaCa ⁷⁰	8333.44–8678.90	182/182/0	5.0×10^{-4}	7.3×10^{-4}	AFGL
15PeSoSoLy ⁶²	9378.84–9427.02	41/41/0	9.9×10^{-4}	3.1×10^{-3}	AFGL
16SeSiLuBo ⁶⁶	11,374.09–11,422.29	43/43/0	9.9×10^{-3}	9.9×10^{-3}	AFGL
13PaLiLuLi ⁵⁶	12,504.90–12,676.68	132/132/0	3.5×10^{-3}	3.5×10^{-3}	AFGL

^aA/V/D = Available/Validated/Deleted transitions.

^bCSU = Average claimed source uncertainty.

^cMSU = Average MARVEL-suggested source uncertainty.

FIGURE 2 Coverage of the transitions data of ¹⁶O¹²C¹⁸O obtained from literature sources (see Table 1 for more details about the sources). The green columns follow the left vertical axis and each column covers a region of 40 cm⁻¹. In the background, the spectrum from HITRAN 2020⁷⁸ is given in purple, with the right vertical axis being the line intensity.



3.1 | Literature sources utilized

Tags for the literature sources of Table 1 were created following the practice introduced in Reference 93. The first digits of the tag are the final two digits of the publication year of the article. This is followed by the two initial letters of the surname of each of the authors, limited to the first four authors. If the paper is written by a single author, the first eight letters of the complete surname is used. Each line is given a unique tag based on the reference tag and line counting number.

As to the experimental data, 12,362 transitions have been measured only once, while there are one and eight transitions which were measured ten and nine times, respectively. The principal component of the final SN contains 33,459 transitions, while the remaining 184 transitions form 112 floating components, containing 303 energy levels.

The experimentally measured transitions involve 9090 energy levels. We were able to determine empirical energies for 8786 rovibrational quantum states of 628. While in this study, and in our

previous study of the high-resolution spectra of 636,¹⁰ we have adopted the AFGL notation, several articles providing the transitions data utilized different notations, such as the standard (harmonic) notation. These sources can be identified via the last column of Table 1. In such cases and to make all datasets consistent, we matched the lines utilizing the HITRAN⁷⁸ and Ames-2021¹⁵ databases.

Figure 2 illustrates the distribution of the transitions data collected, using two vertical axes to help appreciate the amount of experimental data acquired compared to HITRAN 2020.⁷⁸ One can clearly see that there is still a need for accurate experimental data across the spectrum.

3.2 | Literature sources not utilized

Below we explain why we did not use the data reported in some of the sources during the present MARVEL analysis of the high-resolution spectra of ¹⁶O¹²C¹⁸O.

86EsRo³⁸: The 473 transitions provided by this source are all included in the large compilation of experimental results of 86EsSaRoVa.³⁹

49GoMoMcPi¹⁶: The lines of this source, covering the region 4766–4924 cm⁻¹, have the claimed uncertainty of 0.07 cm⁻¹. This region is well covered by more recent sources having significantly higher accuracy, and no new energy levels are produced from this source.

64BeEg¹⁷: The lines of this source, covering the region 2012–4650 cm⁻¹, have the claimed uncertainty of 0.07 cm⁻¹. This region is well covered by more recent sources having significantly higher resolution, and no new energy levels are produced from this source.

67Hahn²⁰: This source provides the same bands twice in two sets of tables, with the second set of tables switching the assigned branch. Our analysis shows that their tab. I provides the correct assignments. The lines of this source, covering the region around 4.3 μm, have an uncertainty of 0.04 cm⁻¹. This region is well covered by more recent sources having significantly higher accuracy, and no new energy levels are produced from this source.

77SrFiKil²³: This source gives two transitions detected in Raman spectra, which obey different selection rules compared to one-photon transitions. However, they were not used, as they are not fully assigned, that is, no band was provided, and they have a low accuracy of 0.05 cm⁻¹.

08ToBrMiDe⁴⁷: The data provided is cited as coming from other sources; we acquired these data from their original sources.

08WiMaVaPe⁴⁹: Transitions data reported in this source were detected in the atmosphere of Venus. These data need to go through further validation procedures to be included and used in a MARVEL-type analysis.

3.3 | Specific comments on entries of Table 1

80EnYoSaHo²⁶: This source contains five pure rotational transitions, whose measurement in the microwave region was made possible by the non-zero dipole moment, about $7.0(15) \times 10^{-4}$ D,²⁶ of 628, arising due to the substitution of one ¹⁶O with a ¹⁸O atom in carbon dioxide.

68ObRaHaMc²¹: Two separate datasets were provided by two different laboratories, the two datasets were included independently. The dataset labeled 68ObRaHaMc(P) originates from the Pennsylvania laboratory, while the dataset labeled 68ObRaHaMc(O) comes from the Ohio laboratory.

78RoFiBuCa²⁵: This source contains 81 transitions. Our MARVEL analysis suggested that these transitions need to be recalibrated. We found the calibration factor to be 0.99997229.

83EsRo³⁰: Out of the 1042 measured transitions reported, 93 transitions could not be validated, as they form a number of floating components (thus, these transitions could still be correct).

66GoMc¹⁹: The data comes from the thesis 65Gordan.¹⁸

86BrSoFr⁹⁴: This paper presents beat-frequency measurements of transitions belonging to multiple isotopologues of carbon dioxide, as well as highly accurate calculated data in tabs. III–XI. The beat-frequency

measurements cannot be utilized in our current study as they link transitions of different isotopologues. These high-accuracy data could potentially be useful after the construction of a 626 MARVEL set. We are in the process of constructing one. Our current study utilizes only the data presented in tab. V of Reference 94.

4 | RESULTS AND DISCUSSION

4.1 | Relabeling of states

For the sake of unifying the notation of the quantum states of 628 across the entire dataset, we had to update the labels of slightly more than 1000 lines, collected from 11 sources (see Table 1). During the update, we found several lines whose assignment disagreed with the rest of the dataset. To check the assignments, these lines were compared to lines present in the Ames-2021¹⁵ and HITRAN 2020⁷⁸ line lists.

4.2 | Energy levels

As already noted above, our literature search ended up with 19,438 unique experimental transitions. During the validation process only slightly over 100 measured transitions had to be deleted, highlighting how careful the interpretations of high-resolution experimental measurements are for 628. Based on the validated transitions, MARVEL generated 8786 empirical rovibrational energy values. Figure 3 compares the energy-level coverage, as a function of the rotational

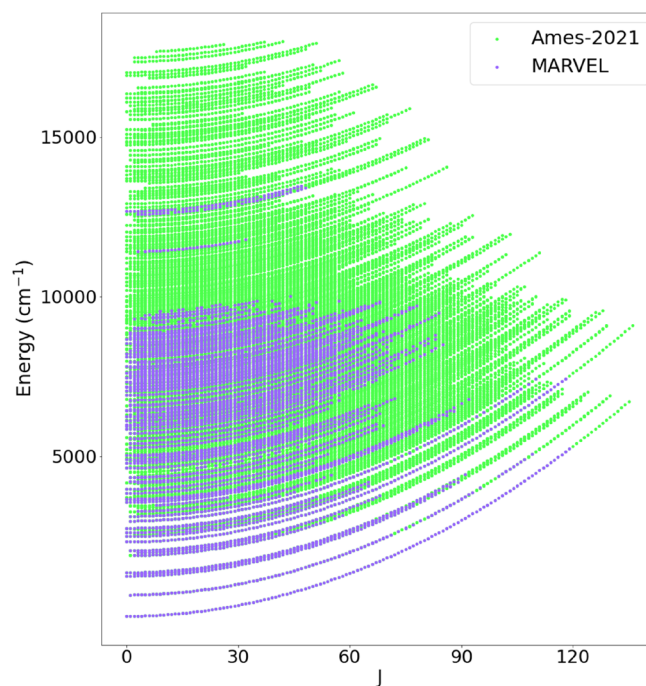


FIGURE 3 Energy-level coverage of the dataset obtained during this study against that of Ames-2021.¹⁵ See Table A1 (Appendix A) for details about the vibrational bands of ¹⁶O¹²C¹⁸O.

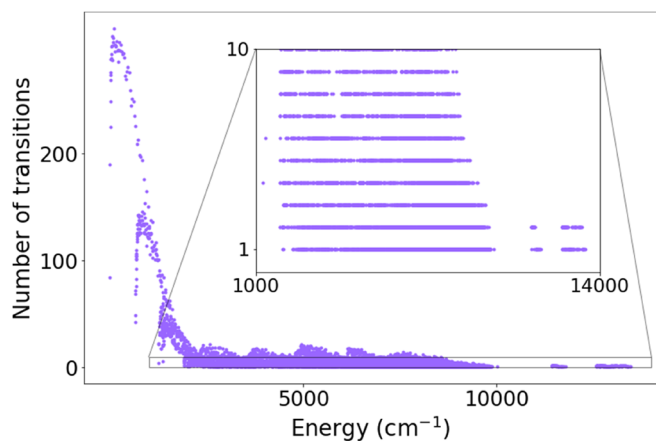


FIGURE 4 Degree distribution of the transitions used for the determination of empirical rovibrational energy level.

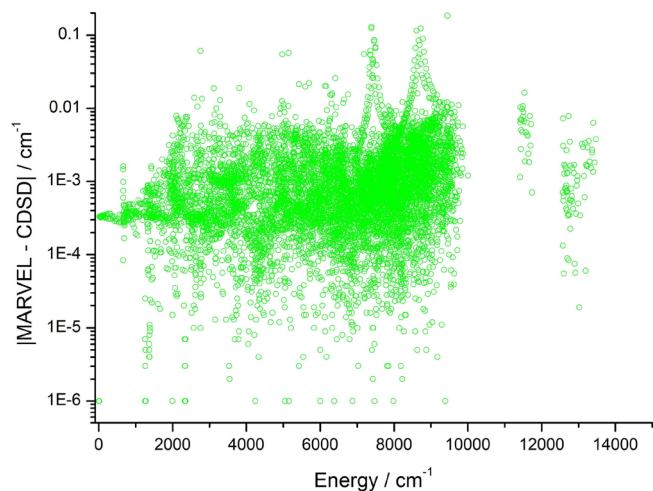


FIGURE 5 A comparison between rovibrational energies of the present dataset and those of CDS-2019,¹⁴ the unit is cm^{-1} . The average absolute difference between MARVEL and CDS-2019 is as small as 0.0017 cm^{-1} . The maximum absolute difference between MARVEL and CDS-2019 is 0.182 cm^{-1} .

quantum number J , of our experimental dataset and that of Ames-2021.¹⁵ Evidently, there is a lack of experimental data above $10,000 \text{ cm}^{-1}$ and at high J values, especially above 7000 cm^{-1} . This calls for laboratory measurements at elevated temperatures.

Figure 4 illustrates the distribution of the transitions used for the determination of each empirical rovibrational energy level. Figure 4 reflects the fact that in experimental spectroscopic networks the degrees of the quantum states display an inverse-power-law-like (i.e., heavy-tailed or near scale-free⁹⁶) distribution.^{81,82} This distribution implies the presence of a small number of high-degree quantum states, called hubs, in the spectroscopic network, as clearly seen in this figure. The highest-degree hubs of $^{16}\text{O}^{12}\text{C}^{18}\text{O}$, which have more than 300 incident transitions, have the label $(J\ 0\ 0\ 0\ 0\ 1\ e)$, with $J = 13\text{--}17, 25$, and 27 .

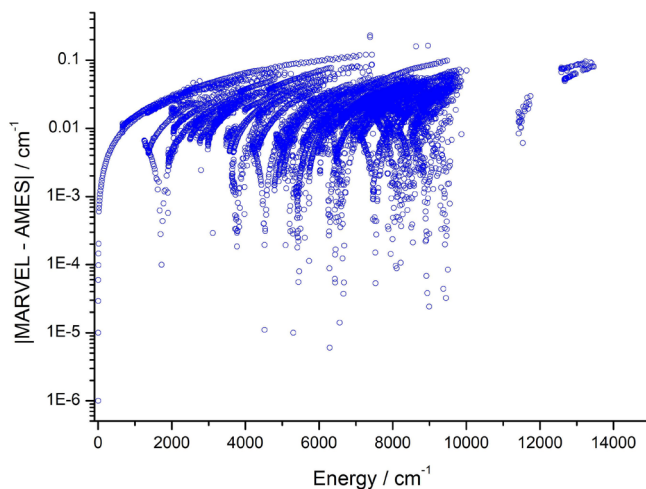


FIGURE 6 A comparison between rovibrational energies of the present dataset and those of Ames-2021,¹⁵ the unit is cm^{-1} . The average absolute difference and the maximum absolute difference between MARVEL and Ames-2021 is 0.022 and 0.230 cm^{-1} , respectively.

In Table A1 (see the Appendix A), one finds information about specific vibrational bands. Note that the maximum value of J , $J_{\text{max}} = 119$, is for the $0\ 0\ 0\ 0\ 1\ e$ ground vibrational state. The rotational coverage of the vibrationally excited bands is usually significantly less than this. The number of vibrational bands covered in this study is 190.

4.3 | Comparison with line lists

Comparisons of our transitions and energy-level data with those in the available line lists, like CDS-2019¹⁴ and Ames-2021,¹⁵ show good overall agreement. Figures 5 and 6 show the absolute differences between the MARVEL data and those in CDS-2019 and Ames-2021, respectively. It should be noted that our data show significantly better agreement with CDS-2019 (0.0017 cm^{-1}) than with Ames-2021 (0.022 cm^{-1}), which is not surprising, since the CDS-2019 data are semi-empirically fitted from experimental data.

As shown in Figure 5, there are energy levels with deviations from the CDS results larger than 0.1 cm^{-1} . Table 2 lists these energy levels. It can be seen that most of these energy levels have high J rotational quantum number, where both the experimental and the effective Hamiltonian results are less reliable. Besides the trivial assignment conflicts, 35 31112 f versus 35 51105 f and 45 10031 e versus 45 09911 e, we found a notable issue: the experimental line position of 13KaCaMoBe.5422 is $6244.7874 \text{ cm}^{-1}$, while the same transition in CDS has a line position of $6244.7732 \text{ cm}^{-1}$ (the aforementioned line positions are not to be confused with the energy values presented in Table 2). Since the 13KaCaMoBe.5422 line is a single transition, MARVEL cannot help to resolve this conflict. It is also important to note that we found several vibrational labels in the AMES database which contain double-digit quantum numbers, for

TABLE 2 Experimental energy levels with discrepancies larger than 0.1 cm^{-1} from the CDSD results.

MARVEL descriptors	MARVEL energy/cm ⁻¹	CDSD energy/cm ⁻¹	Difference/cm ⁻¹	MARVEL unc/cm ⁻¹	Comment
103 00011 e	6231.4872	6231.3828	0.1044	8.423e-03	High- <i>J</i> energy level
104 00011 e	6306.9318	6306.8290	0.1028	6.633e-03	High- <i>J</i> energy level
105 00011 e	6383.0914	6382.9902	0.1012	8.966e-03	High- <i>J</i> energy level
106 00011 e	6459.9729	6459.8663	0.1066	6.797e-03	High- <i>J</i> energy level
107 00011 e	6537.5603	6537.4568	0.1035	8.953e-03	High- <i>J</i> energy level
108 00011 e	6615.8710	6615.7615	0.1095	6.870e-03	High- <i>J</i> energy level
109 00011 e	6694.8860	6694.7801	0.1059	9.017e-03	High- <i>J</i> energy level
110 00011 e	6774.6247	6774.5123	0.1124	6.907e-03	High- <i>J</i> energy level
111 00011 e	6855.0666	6854.9577	0.1089	9.040e-03	High- <i>J</i> energy level
112 00011 e	6936.2314	6936.1161	0.1153	6.936e-03	High- <i>J</i> energy level
113 00011 e	7018.0994	7017.9870	0.1124	9.420e-03	High- <i>J</i> energy level
114 00011 e	7100.6886	7100.5706	0.1180	6.972e-03	High- <i>J</i> energy level
116 00011 e	7267.9926	7267.8726	0.1200	7.246e-03	High- <i>J</i> energy level
35 51105 f	7389.2683	7389.4869	0.2186	1.157e-03	Mislabeled with 35 31112 f
35 31112 f	7389.4903	7389.2595	0.2309	1.157e-03	Mislabeled with 35 51105 f
118 00011 e	7438.1397	7438.0201	0.1196	8.390e-03	High- <i>J</i> energy level
37 41113 f	8638.2085	8638.0495	0.1589	1.744e-03	Conflict: 13KaCaMoBe.5422 versus CDSD
45 10031 e	8964.4721	8964.6356	0.1635	2.027e-03	Mislabeled in CDSD as 45 09911 e

example, $v_2 = 14$, which is unusual for CO_2 . These labels are not the same as the MARVEL labels; thus, these transitions have been excluded from the comparison presented.

5 | SUMMARY AND CONCLUSIONS

This paper describes a comprehensive analysis, employing the MARVEL algorithm and code,⁷³⁻⁷⁵ of the high-resolution, rovibrational spectroscopy literature available for the third most abundant isotopologue of carbon dioxide, $^{16}\text{O}^{12}\text{C}^{18}\text{O}$. Assigned transitions have been extracted from altogether 52 literature sources (there are seven more sources containing rovibrational transitions data about $^{16}\text{O}^{12}\text{C}^{18}\text{O}$ but for various reasons these data have not been utilized during the present study). The great majority of the transitions were verified using appropriate selection rules, tools provided by the network-theoretical algorithms MARVEL utilizes, and a comparative analysis against data available in the form of line lists. These extensive comparisons helped to ensure the consistency of the labeling of the quantum states involved in the measured transitions.

The transitions data validated for $^{16}\text{O}^{12}\text{C}^{18}\text{O}$ cover the wavenumber range of $2\text{--}12,676\text{ cm}^{-1}$. The experimental transitions, of which there are 19,438 unique ones, yield 8786 empirical rovibrational energy levels. Estimates are provided for the uncertainties of the empirical energies, based on the experimental uncertainties of the transitions and the bootstrap technique. The detailed analysis of the present study reveals areas in the spectrum where there is a lack of experimental data.

Comparison with the CDSD-2019 database¹⁴ reveals a small number of differences between the energy levels of the two databases. Most of the discrepancies are either for energy levels with high *J* rotational quantum number or energy levels defined by the 13KaCaMoBe⁵⁵ source. We do not know whether CDSD-2019 utilized this source or not. In the latter case we recommend that the next version of CDSD should include these measurement results. A comparison between our energy levels and those of Ames-2021¹⁵ and CDSD-2019¹⁴ shows significantly better agreement with CDSD-2019. This observation highlights the importance of fitting theoretical models using available experimental data. There are plans to carry out further research in our groups to analyze, with the aid of the MARVEL procedure, more isotopologues of CO_2 , including the parent one. These collectively will be used to give improved line lists for isotopologues of this important molecule.

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DATA AVAILABILITY STATEMENT

The data that supports the findings of this study are available in the supplementary material of this article.

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APPENDIX A

TABLE A1 Vibrational bands of $^{16}\text{O}^{12}\text{C}^{18}\text{O}$ investigated in this study with an ordering based on band descriptors.

Band	Range of J	Nb. of energy levels	Unc. range/ cm^{-1}	Avg. unc./ cm^{-1}	Range of energy levels/ cm^{-1}
0 0 0 1 e	0-119	120	0.0000-0.0096	0.0020	0.0000-5233.4864
0 0 0 1 1 e	0-118	119	0.0000-0.0091	0.0019	2332.1126-7438.1397
0 0 0 2 1 e	0-68	69	0.0000-0.0012	0.0002	4639.5011-6337.2420
0 0 0 3 1 e	0-84	85	0.0003-0.0035	0.0008	6922.1967-9483.0059
0 0 0 4 1 e	7-41	22	0.0010-0.0011	0.0010	9200.2034-9793.9610
0 0 0 5 1 e	3-32	28	0.0080-0.0160	0.0083	11,417.8923-11,787.0476
0 1 1 0 1 e	1-109	93	0.0005-0.0093	0.0019	663.1091-5064.6047
0 1 1 0 1 f	1-104	89	0.0005-0.0082	0.0016	663.1132-4679.1109
0 1 1 1 1 e	1-110	92	0.0005-0.0096	0.0021	2982.8414-7429.8112
0 1 1 1 1 f	1-105	88	0.0005-0.0082	0.0017	2982.8434-7043.7292
0 1 1 2 1 e	1-46	45	0.0005-0.0017	0.0007	5277.8754-6061.0981
0 1 1 2 1 f	1-43	42	0.0005-0.0016	0.0006	5277.8793-5964.2518
0 1 1 3 1 e	1-76	71	0.0010-0.0064	0.0014	7548.2468-9650.1290
0 1 1 3 1 f	1-74	69	0.0010-0.0032	0.0013	7548.2480-9544.6214
0 2 2 0 1 e	2-78	75	0.0005-0.0057	0.0017	1327.3639-3597.5626
0 2 2 0 1 f	2-88	69	0.0008-0.0068	0.0022	1327.3640-4212.0507
0 2 2 1 1 e	2-79	73	0.0007-0.0056	0.0020	3634.7302-5945.0836
0 2 2 1 1 f	2-87	68	0.0012-0.0067	0.0024	3634.7302-6432.8821
0 2 2 3 1 e	2-59	55	0.0011-0.0058	0.0019	8175.4856-9449.7232
0 2 2 3 1 f	2-59	51	0.0016-0.0040	0.0020	8175.4856-9449.7346
0 3 3 0 1 e	3-43	39	0.0005-0.0040	0.0020	1992.7491-2688.3502
0 3 3 0 1 f	3-38	34	0.0005-0.0051	0.0028	1992.7516-2536.7277
0 3 3 3 1 e	4-42	34	0.0007-0.0039	0.0022	8806.7913-9452.4713
0 3 3 3 1 f	4-37	30	0.0011-0.0050	0.0028	8806.7939-9307.9306
1 0 0 0 1 e	0-91	83	0.0000-0.0066	0.0008	1365.8435-4443.9265
1 0 0 0 2 e	0-89	85	0.0000-0.0052	0.0007	1259.4256-4199.4066
1 0 0 1 1 e	0-92	87	0.0000-0.0068	0.0006	3675.1324-6795.6258
1 0 0 1 2 e	0-88	85	0.0000-0.0049	0.0005	3571.1398-6423.8802
1 0 0 2 1 e	0-69	70	0.0010-0.0016	0.0010	5959.9536-7709.1259
1 0 0 2 2 e	0-85	82	0.0010-0.0036	0.0012	5858.0251-8500.5825
1 0 0 3 1 e	0-64	64	0.0010-0.0015	0.0010	8220.3567-9714.9192
1 0 0 3 2 e	0-68	67	0.0010-0.0015	0.0010	8120.1019-9804.7857
1 0 0 5 1 e	0-47	46	0.0030-0.0060	0.0031	12,668.1363-13,465.7561
1 0 0 5 2 e	3-48	41	0.0030-0.0077	0.0035	12,574.1883-13,402.0744
1 1 1 0 1 e	1-68	68	0.0001-0.0023	0.0007	2050.0758-3776.4846
1 1 1 0 1 f	1-55	53	0.0001-0.0057	0.0008	2050.0769-3186.4135
1 1 1 0 2 e	2-58	55	0.0001-0.0014	0.0008	1903.9476-3161.2710
1 1 1 0 2 f	2-47	46	0.0005-0.0019	0.0009	1903.9494-2734.2130
1 1 1 1 1 e	1-67	66	0.0005-0.0034	0.0008	4346.9204-6010.2858
1 1 1 1 1 f	1-67	66	0.0005-0.0037	0.0008	4346.9162-6014.1590
1 1 1 1 2 e	1-69	68	0.0005-0.0032	0.0008	4201.8804-5964.5091
1 1 1 1 2 f	1-67	67	0.0005-0.0036	0.0008	4201.8846-5868.0670
1 1 1 2 1 e	1-67	66	0.0010-0.0010	0.0010	6619.2809-8269.5815

TABLE A1 (Continued)

Band	Range of <i>J</i>	Nb. of energy levels	Unc. range/cm ⁻¹	Avg. unc./cm ⁻¹	Range of energy levels/cm ⁻¹
1 1 1 2 1 f	1-70	67	0.0010-0.0012	0.0010	6619.2834-8423.3825
1 1 1 2 2 e	1-67	67	0.0010-0.0028	0.0011	6476.5367-8126.5302
1 1 1 2 2 f	1-70	70	0.0010-0.0063	0.0013	6476.5369-8279.9376
1 1 1 3 1 e	1-51	42	0.0010-0.0023	0.0012	8867.2147-9820.4597
1 1 1 3 1 f	1-49	45	0.0010-0.0020	0.0012	8867.2189-9749.7059
1 1 1 3 2 e	1-49	46	0.0011-0.0038	0.0012	8726.4635-9607.2456
1 1 1 3 2 f	2-50	46	0.0011-0.0050	0.0013	8727.9063-9645.0928
1 2 2 0 1 e	9-49	23	0.0011-0.0018	0.0012	2761.4504-3633.1359
1 2 2 0 1 f	8-47	31	0.0011-0.0150	0.0017	2754.8577-3561.6412
1 2 2 0 2 e	9-26	8	0.0020-0.0020	0.0020	2582.6529-2808.8128
1 2 2 0 2 f	9-26	7	0.0020-0.0021	0.0020	2582.6525-2808.8147
1 2 2 1 1 e	2-60	52	0.0014-0.0037	0.0017	5014.8219-6353.4478
1 2 2 1 1 f	2-58	51	0.0014-0.0043	0.0019	5014.8218-6266.5610
1 2 2 1 2 e	2-45	40	0.0014-0.0026	0.0016	4838.7587-5595.3077
1 2 2 1 2 f	2-49	38	0.0014-0.0039	0.0017	4838.7586-5734.4743
1 2 2 2 1 e	2-53	49	0.0011-0.0029	0.0012	7274.7261-8313.1711
1 2 2 2 1 f	2-55	52	0.0011-0.0017	0.0012	7274.7281-8392.4841
1 2 2 2 2 e	2-55	52	0.0011-0.0024	0.0013	7101.2135-8219.1860
1 2 2 2 2 f	2-50	47	0.0011-0.0035	0.0015	7101.2140-8026.5629
1 2 2 3 1 e	9-25	7	0.0017-0.0018	0.0017	9540.5545-9742.7194
1 2 2 3 1 f	9-24	7	0.0017-0.0018	0.0018	9540.5549-9724.6733
1 2 2 3 2 e	8-27	14	0.0017-0.0018	0.0017	9362.8399-9609.8720
1 2 2 3 2 f	7-26	15	0.0017-0.0018	0.0018	9357.0576-9590.3736
1 3 3 2 1 e	3-40	25	0.0017-0.0024	0.0018	7928.6463-8521.9960
1 3 3 2 1 f	3-40	24	0.0017-0.0026	0.0018	7928.6464-8521.9873
1 3 3 2 2 e	4-33	27	0.0011-0.0036	0.0023	7732.6129-8134.4702
1 3 3 2 2 f	4-33	27	0.0011-0.0048	0.0029	7732.6155-8134.4694
1 8 8 1 1 f	35-35	1	0.0017-0.0017	0.0017	9450.9030-9450.9030
2 0 0 0 1 e	0-51	52	0.0003-0.0003	0.0003	2757.1783-3735.2672
2 0 0 0 2 e	0-65	66	0.0001-0.0015	0.0003	2614.2479-4189.8779
2 0 0 0 3 e	0-65	65	0.0001-0.0033	0.0004	2500.7602-4078.7086
2 0 0 1 1 e	0-65	66	0.0000-0.0010	0.0002	5042.5813-6611.7206
2 0 0 1 2 e	0-72	73	0.0000-0.0021	0.0002	4904.8594-6819.5761
2 0 0 1 3 e	0-67	67	0.0000-0.0018	0.0002	4791.2595-6454.3905
2 0 0 2 1 e	1-60	59	0.0005-0.0011	0.0009	7304.3916-8631.8830
2 0 0 2 2 e	0-69	67	0.0005-0.0016	0.0007	7171.0199-8916.6854
Band	Range of <i>J</i>	Nb. of energy levels	Unc. range	Avg. of unc.	Range of energy levels
2 0 0 2 3 e	0-56	57	0.0010-0.0012	0.0010	7056.8639-8214.0537
2 0 0 3 2 e	5-35	29	0.0003-0.0029	0.0009	9423.5275-9864.9947
2 0 0 3 3 e	2-44	28	0.0010-0.0013	0.0010	9299.7610-10,010.3913
2 1 1 0 1 e	8-27	20	0.0011-0.0024	0.0013	3480.4472-3732.6282
2 1 1 0 1 f	9-27	19	0.0011-0.0017	0.0011	3487.1981-3733.5956
2 1 1 0 2 e	3-55	51	0.0001-0.0109	0.0006	3285.4403-4413.7777
2 1 1 0 2 f	4-46	43	0.0011-0.0033	0.0012	3288.3994-4078.6295
2 1 1 0 3 e	1-45	44	0.0011-0.0055	0.0013	3128.0899-3889.8065

(Continues)

TABLE A1 (Continued)

Band	Range of <i>J</i>	Nb. of energy levels	Unc. range	Avg. of unc.	Range of energy levels
2 1 1 0 3 f	6–43	37	0.0011–0.0027	0.0012	3142.8827–3826.3196
2 1 1 1 1 e	1–52	51	0.0005–0.0018	0.0007	5727.7587–6734.8445
2 1 1 1 1 f	1–48	47	0.0005–0.0017	0.0007	5727.7629–6590.0078
2 1 1 1 2 e	1–55	55	0.0005–0.0017	0.0006	5559.2934–6682.5682
2 1 1 1 2 f	1–55	55	0.0005–0.0015	0.0006	5559.2944–6685.6383
2 1 1 1 3 e	1–53	52	0.0005–0.0017	0.0006	5406.7995–6452.1156
2 1 1 1 3 f	1–54	52	0.0005–0.0030	0.0008	5406.8036–6494.6162
2 1 1 2 1 e	1–46	40	0.0010–0.0043	0.0012	7976.6084–8760.5051
2 1 1 2 1 f	2–51	39	0.0010–0.0040	0.0013	7978.0662–8941.1357
2 1 1 2 2 e	1–63	62	0.0010–0.0041	0.0011	7812.3730–9271.0619
2 1 1 2 2 f	1–60	57	0.0010–0.0019	0.0011	7812.3754–9140.0982
2 1 1 2 3 e	1–56	55	0.0010–0.0018	0.0010	7660.7226–8817.7830
2 1 1 2 3 f	1–52	50	0.0010–0.0027	0.0011	7660.7237–8662.6350
2 2 2 1 1 e	3–55	42	0.0010–0.0026	0.0014	6409.9895–7534.8650
2 2 2 1 1 f	3–25	18	0.0017–0.0025	0.0019	6409.9895–6644.1362
2 2 2 1 2 e	3–73	51	0.0010–0.0031	0.0014	6215.4779–8187.6136
2 2 2 1 2 f	3–35	29	0.0017–0.0025	0.0018	6215.4780–6672.8150
2 2 2 1 3 e	2–50	44	0.0010–0.0031	0.0014	6031.2460–6964.3008
2 2 2 1 3 f	2–28	22	0.0017–0.0018	0.0018	6031.2459–6327.0191
2 2 2 2 2 e	5–45	36	0.0011–0.0031	0.0012	8462.3978–9204.0100
2 2 2 2 2 f	2–43	31	0.0011–0.0018	0.0012	8453.6642–9139.3721
3 0 0 0 1 e	3–27	25	0.0010–0.0020	0.0010	4172.3395–4447.1881
3 0 0 0 2 e	0–54	55	0.0001–0.0020	0.0005	3987.5967–5080.4741
3 0 0 0 3 e	0–50	51	0.0001–0.0010	0.0002	3856.7644–4792.5262
3 0 0 1 1 e	0–70	70	0.0010–0.0016	0.0010	6429.1719–8249.8435
3 0 0 1 2 e	0–83	80	0.0003–0.0022	0.0007	6254.5904–8797.3658
3 0 0 1 3 e	0–83	81	0.0002–0.0022	0.0007	6127.7813–8662.8739
3 0 0 1 4 e	0–71	71	0.0006–0.0012	0.0010	5993.5823–7861.7690
3 0 0 2 2 e	3–37	32	0.0005–0.0013	0.0007	8501.8048–9006.7226
3 0 0 2 3 e	2–42	40	0.0005–0.0013	0.0006	8376.3986–9027.0713
3 0 0 2 4 e	7–32	17	0.0010–0.0012	0.0010	8258.2346–8621.7103
3 1 1 0 3 e	12–49	20	0.0030–0.0030	0.0030	4562.2856–5405.3103
3 1 1 0 4 e	2–58	57	0.0020–0.0034	0.0021	4342.0294–5600.2067
3 1 1 0 4 f	1–44	33	0.0020–0.0025	0.0020	4340.5608–5072.2893
3 1 1 1 1 e	1–67	63	0.0011–0.0028	0.0012	7123.3779–8789.3006
3 1 1 1 1 f	1–63	60	0.0011–0.0023	0.0012	7123.3822–8603.9812
3 1 1 1 2 e	1–72	69	0.0011–0.0055	0.0014	6928.3093–8844.8662
3 1 1 1 2 f	1–76	69	0.0011–0.0150	0.0016	6928.3118–9069.6429
3 1 1 1 3 e	1–74	69	0.0011–0.0064	0.0014	6763.4044–8784.5915
3 1 1 1 3 f	1–64	61	0.0011–0.0026	0.0012	6763.4064–8283.8628
3 1 1 1 4 e	1–57	56	0.0010–0.0017	0.0011	6598.4373–7806.3515
3 1 1 1 4 f	1–63	60	0.0011–0.0023	0.0012	6598.4394–8077.0350
3 2 2 0 4 e	4–59	34	0.0021–0.0021	0.0021	4971.8332–6273.2620
3 2 2 0 4 f	9–62	33	0.0021–0.0023	0.0021	4997.7368–6407.9057
3 2 2 1 1 e	2–49	43	0.0010–0.0024	0.0012	7812.5635–8709.8945
3 2 2 1 1 f	2–43	41	0.0010–0.0036	0.0015	7812.5635–8505.4690

TABLE A1 (Continued)

Band	Range of <i>J</i>	Nb. of energy levels	Unc. range	Avg. of unc.	Range of energy levels
3 2 2 1 2 e	3-50	45	0.0017-0.0033	0.0018	7599.2614-8528.9869
3 2 2 1 2 f	3-56	49	0.0013-0.0040	0.0020	7599.2612-8764.2334
3 2 2 1 3 e	2-60	51	0.0011-0.0028	0.0018	7403.7187-8741.2730
3 2 2 1 3 f	2-50	48	0.0017-0.0035	0.0020	7403.7186-8335.3655
3 2 2 1 4 e	2-52	41	0.0011-0.0028	0.0017	7212.8681-8222.4735
3 2 2 1 4 f	3-57	37	0.0017-0.0040	0.0020	7215.0715-8423.7931
4 0 0 5 e	36-56	14	0.0021-0.0025	0.0021	5425.1265-6110.8390
4 0 0 1 1 e	0-52	53	0.0010-0.0017	0.0010	7830.1936-8841.8785
4 0 0 1 2 e	0-62	63	0.0005-0.0012	0.0008	7625.5519-9053.7986
4 0 0 1 3 e	0-78	78	0.0005-0.0016	0.0008	7465.0986-9706.8034
4 0 0 1 4 e	0-63	64	0.0005-0.0010	0.0006	7338.7755-8806.6931
4 0 0 1 5 e	0-67	63	0.0005-0.0012	0.0009	7181.2141-8848.8219
4 1 1 0 1 e	8-49	35	0.0010-0.0019	0.0010	6332.5294-7209.2689
4 1 1 0 3 e	15-57	21	0.0010-0.0011	0.0010	5976.5605-7102.1309
4 1 1 0 4 e	6-67	53	0.0010-0.0014	0.0010	5734.9692-7391.8487
4 1 1 0 5 e	24-57	9	0.0020-0.0021	0.0020	5761.7669-6758.7959
4 1 1 1 1 e	5-38	29	0.0011-0.0022	0.0012	8541.5124-9073.8383
4 1 1 1 1 f	5-39	31	0.0011-0.0019	0.0012	8541.5635-9105.0090
4 1 1 1 2 e	1-56	50	0.0010-0.0027	0.0012	8311.3431-9476.5311
4 1 1 1 2 f	2-58	54	0.0010-0.0015	0.0011	8312.8118-9566.1302
4 1 1 1 3 e	1-66	59	0.0007-0.0026	0.0012	8124.3083-9734.2354
4 1 1 1 3 f	1-68	62	0.0007-0.0038	0.0014	8124.3075-9839.2444
4 1 1 1 4 e	1-57	54	0.0007-0.0020	0.0011	7957.7658-9161.9376
4 1 1 1 4 f	3-55	51	0.0007-0.0030	0.0013	7961.4266-9084.1082
4 1 1 1 5 e	1-52	44	0.0011-0.0017	0.0012	7778.1931-8786.2623
4 1 1 1 5 f	4-50	45	0.0011-0.0020	0.0012	7784.8259-8715.3066
4 2 2 0 2 e	12-40	19	0.0011-0.0011	0.0011	6829.2595-7377.3039
4 2 2 0 2 f	9-36	14	0.0011-0.0012	0.0011	6804.8647-7263.7893
4 2 2 0 4 e	11-56	20	0.0011-0.0017	0.0011	6407.1734-7535.9426
4 2 2 0 4 f	11-46	14	0.0011-0.0011	0.0011	6407.1721-7156.2429
4 2 2 1 2 e	2-24	15	0.0017-0.0022	0.0018	8991.3899-9209.1369
4 2 2 1 2 f	2-26	20	0.0017-0.0023	0.0018	8991.3899-9246.5826
4 2 2 1 3 e	2-39	30	0.0017-0.0023	0.0018	8780.9258-9349.8868
4 2 2 1 3 f	2-45	28	0.0017-0.0030	0.0019	8780.9258-9536.5767
4 2 2 1 4 e	2-37	19	0.0017-0.0019	0.0018	8585.6536-9098.6729
4 2 2 1 4 f	2-30	28	0.0017-0.0019	0.0018	8585.6536-8924.3010
4 2 2 1 5 f	8-20	12	0.0017-0.0032	0.0019	8408.7969-8536.7997
5 0 0 3 e	1-51	51	0.0010-0.0012	0.0010	6596.4069-7571.2185
5 0 0 4 e	0-60	52	0.0010-0.0030	0.0010	6442.9762-7782.8251
5 0 0 5 e	1-54	40	0.0010-0.0015	0.0010	6307.0880-7397.1086
5 0 0 6 e	2-37	29	0.0010-0.0013	0.0010	6131.8625-6649.5142
5 0 0 1 2 e	2-41	37	0.0010-0.0023	0.0011	9015.3934-9644.3095
5 0 0 1 3 e	1-49	45	0.0010-0.0013	0.0010	8820.6254-9713.5475
5 0 0 1 4 e	0-57	51	0.0005-0.0012	0.0008	8672.6893-9873.3666
5 0 0 1 5 e	0-50	47	0.0005-0.0014	0.0007	8535.2998-9465.4914
5 0 0 1 6 e	3-40	25	0.0010-0.0019	0.0011	8361.1899-8958.8273

(Continues)

TABLE A1 (Continued)

Band	Range of <i>J</i>	Nb. of energy levels	Unc. range	Avg. of unc.	Range of energy levels
5 1 1 0 2 e	8–50	31	0.0010–0.0010	0.0010	7527.2603–8439.2338
5 1 1 0 5 e	36–39	4	0.0011–0.0011	0.0011	7413.5719–7497.4103
5 1 1 0 5 f	33–36	4	0.0011–0.0011	0.0011	7338.4189–7416.0128
5 1 1 1 2 f	35–35	1	0.0011–0.0011	0.0011	7389.2686–7389.2686
5 1 1 1 4 e	4–27	11	0.0011–0.0017	0.0013	9321.2887–9589.3043
5 1 1 1 4 f	9–28	9	0.0012–0.0012	0.0012	9346.9260–9611.0145
5 1 1 1 5 e	8–33	8	0.0011–0.0014	0.0012	9167.2343–9550.3074
5 1 1 1 5 f	14–35	8	0.0012–0.0014	0.0013	9217.9699–9602.8451
6 0 0 0 4 e	3–39	34	0.0010–0.0013	0.0010	7811.5569–8379.3773
6 0 0 0 5 e	3–47	41	0.0010–0.0016	0.0010	7668.1859–8489.0245
6 0 0 0 6 e	5–34	11	0.0010–0.0010	0.0010	7521.5189–7948.5117